Coupling Between Component Sizing and Regulation Capability in Microgrids

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Abstract—Increasing energy security and reliability concerns are intensifying the interest in microgrids. In this setting, design optimization is vital to achieve a reliable infrastructure without overbuilding. This paper considers the impact of frequency and voltage regulation on the optimal design of a conceptual, autonomous military microgrid. This microgrid comprises a solar panel and vehicles as power sources, with each vehicle incorporating a battery and generator. The power output and terminal voltage of these inverter-based sources must be regulated. The paper investigates the effects of battery DC voltage variations on the decentralized regulation scheme, and the resulting influence on optimal component sizing. To this end, controllers are designed based on the typical assumption that the voltage on the DC side of each inverter is constant. The battery internal resistance is then considered and its impact on regulation performance is investigated. The results show that the battery internal resistance can affect the performance of both frequency and voltage regulation, and consequently must be taken into account in component sizing decisions. Thus, the paper identifies an important coupling between regulation and component sizing problems through battery characteristics, and highlights the need for a combined sizing and regulation framework for microgrid design.

Index Terms—Batteries, frequency control, inverters, microgrids, voltage control.

I. INTRODUCTION

MICROGRIDS are collections of electrical loads and micro-sources functioning as a single system that can operate either in connection with a larger power grid or completely autonomously [1]. They have been attracting much research interest due to their potential to increase energy security and reliability, as well as foster the penetration of distributed renewable resources (e.g., wind, solar) and distributed storage (e.g., plug-in vehicles, community energy storage) [2]–[11]. Because of this potential, the U.S. Department of Defense (DoD) is interested in microgrids as indicated by the SPIDERS (Smart Power Infrastructure Demonstration for Energy Reliability and Security) project, which aims to demonstrate the first complete DoD installation with a secure microgrid capable of islanding.

Whereas the SPIDERS project presents an example microgrid that can operate in both grid-connected and islanded mode, forward operating bases (FOBs)—military bases temporarily established to support tactical operations—exemplify the need for maximizing operational autonomy. Traditionally, these microgrids have relied entirely on diesel generators, whose transportation and fuel re-supply increase the vulnerability of the FOB and the supply lines themselves. Indeed, electric power generation can account for over 70% of fuel consumption at or near the tactical edge [12], and the U.S. Army indicates that 50% of the casualties during resupply missions in Iraq and Afghanistan are due to fuel delivery [13].

To make FOBs more autonomous, the microgrid can leverage local renewable resources and military vehicles with on-board electrical generation and energy storage capability. Such a concept FOB considered in this paper is shown in Fig. 1. Instead of relying entirely on stationary generators, it integrates into the microgrid a solar panel and a fleet of vehicles, each with a battery and on-board generator. Military vehicles in a FOB require significant on-board electric power generation and storage to supply electrical equipment such as radars, radios, and computers. For strategic reasons, it is necessary to supply this power with either minimum idling of the main propulsion engines or in silent watch.

With this military application in mind, this paper is concerned with optimal design of microgrids considering two different aspects: component sizing and regulation. One important aspect of microgrid design is the sizing of its components. While component sizing is often performed based on the expected peak load of the microgrid, it has also been recognized that this approach may be highly conservative and sub-optimal, as many components will be larger than necessary. Power dispatch control strategies can be used to reduce this conservatism, but at the cost of coupling the optimal sizing and dispatch problems [14]–[23]. On the other hand, the regulation problem focuses on controlling the voltage and frequency in the microgrid.

Two types of sources in the example microgrid, the solar panel and the batteries in the plug-in vehicle fleet, are DC and need an inverter interface to connect to an AC microgrid (e.g.,

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It was assumed that the derating factor of optimal sizing and dispatch study for the example microgrid significantly affects the component sizing and regulation problems. An example microgrid was used to show that the coupling between the sizing and regulation problems can indeed be seen in Fig. 1 as a case study to show that the fast-time-scale regulation and slow-time-scale sizing problems, which traditionally have been studied independently due to the disparity of their time scales. 

This framework is applied to the military microgrid example due to a sand storm or destruction of part of the solar panel. The power output from the solar panel was calculated as the product of rated power, a derating factor, and the ratio of incident solar irradiance to the peak solar irradiance of 1 kW/m². It was assumed that the derating factor of the PV array was maintained at 95% with a good maximum power point tracking control algorithm. The optimization resulted in a solar panel of 89 kW, a total of 8.4 kWh battery capacity, a total of 120 kW plug-in vehicle generator power (30 kW per vehicle). It also resulted in an optimal power dispatch strategy for an entire year.

Worst case scenarios, from a regulation perspective, occur when generation or load undergoes a step (or rapid) change, introducing a sizeable mismatch between generation and consumption. Fig. 4 illustrates the hourly load and generation trajectories, for the example microgrid, for one of the days on which a worst-case transient occurred. The shaded region shows an abrupt drop in solar power. The generators were initially idle as there was sufficient solar power to supply the loads and charge the batteries. A 50 kW drop then occurred in the solar power (e.g., due to cloud cover), requiring the batteries and generators to support the loads and stabilize the microgrid. As can be seen in Fig. 4, the resulting optimal hourly sequence of dispatch commands involved the simultaneous increase of battery and generator power.

For the purposes of this paper, it is assumed that a drop of this magnitude could happen instantaneously and unexpectedly, for example due to a sand storm or destruction of part of the solar panel array, and hence it is referred to as the worst-case scenario.

Fig. 1. Example conceptual military microgrid considered in this study for a forward operating base (FOB). The power sources consist of a solar panel array and a fleet of electrified vehicles.

Fig. 2. Inverter-grid interface model.

Fig. 3. The integrated optimal microgrid design framework employed in this study.
Fig. 4. The power profiles for the day that contains the worst-case scenario considered in this paper (the shaded region).

III. MICROGRID REGULATION

This section describes the regulation aspect of the integrated framework of Fig. 3 in detail. The worst-case scenario identified in the previous section defines the microgrid operating conditions and disturbances that is considered.

A. Modeling the Microgrid

The microgrid in Fig. 1 consists of four buses: Two of them are connected to loads; one is connected to an intermittent power source, namely, the solar panel; and one is connected to a re-configurable energy storage and power source, namely, a group of vehicles. The grid is modeled as shown in Fig. 5. For the purposes of this paper, the vehicles are aggregated into a single generator and battery that are controlled independently. The vehicles are assumed to be always available for supporting the microgrid. Furthermore, within the short time scale of interest (i.e., seconds), the number of vehicles connected to the microgrid is assumed to remain constant, leading to a constant generator and battery size. The loads are assumed critical and hence no load-side power management (e.g., load shedding) is considered in this paper.

The solar panel and battery are interfaced with the AC microgrid through inverters. A model for the inverter-grid interface is shown in Fig. 2. The inverter is controlled to regulate the voltage $V_t$ at the terminal bus and active power output $P_{out}$ to the grid. This is achieved by controlling the modulation index $m$ of the inverter, which effectively controls the inverter voltage magnitude $V_t$ through the relationship

$$V_t = m \frac{V_{dc}}{V_{base}}, \quad (1)$$

and the inverter firing angle, which effectively determines the phase angle $\delta_t$. In (1), $V_{base}$ is the base unit voltage that is used for normalization to allow working with the per-unit system [28], and $V_{dc}$ is the DC voltage on the DC terminals of the inverter, which is established by the DC power source. The modulation index $m$ is constrained by a saturation limit $m \leq 1$, so it cannot compensate for arbitrarily low DC voltages.

This paper considers a phase-locked loop (PLL) based inverter control strategy as proposed in [24]. The PLL tracks the AC voltage waveform at the inverter terminals to establish an angle reference signal for the inverter firing circuitry [29]. As a by-product, it also provides an estimate of the local frequency. The power delivered to the microgrid is regulated by controlling the phase $\delta_t$ of the inverter-synthesized voltage waveforms relative to the PLL reference. The dynamics of the inverter controller are given by the following set of differential-algebraic equations:

$$\dot{\theta} = K_2 (P_{set} - P_{out}) - \epsilon \dot{\gamma}, \quad (2b)$$

$$\dot{\delta}_p = \omega_p, \quad (2d)$$

$$0 = V_t - \frac{mV_{dc}}{V_{base}}, \quad (2h)$$

$$0 = P_{out} - \frac{V_{dc}I_{inv}}{P_{base}}, \quad (2h)$$

Equations (2a) and (2b) correspond to integral control of $V_t$ and $P_{out}$, where $V_{set}$ and $P_{set}$ are the desired values for $V_t$ and $P_{out}$, respectively. Equations (2c) and (2d) together describe the PLL dynamics, which, in addition to integral control, also involves damping due to the term $K_d \delta$ in the definition of the auxiliary variable $a$ (2g). The variable $\delta_p$ gives the PLL phase angle, and its time derivative $\omega_p$ provides an estimate of the deviation of system frequency from nominal. The integral action in (2c) aims to drive the difference between the PLL phase angle $\delta_p$ and the terminal phase angle $\delta_t$ to zero. Further details of this PLL model can be found in [24], [29]. Equations (2f) and (2g) define the variables $\theta$ and $a$, respectively. Equation (2h) describes the active power balance between the AC and DC side of the inverter, with $I_{inv}$ representing the inverter DC current. Finally, (2i) gives the active power delivered to the grid. The block diagram shown in Fig. 6 illustrates the interaction between the PLL and the power control scheme.

In this study, (2) is used to model the inverters for both the solar panel and the battery. In addition to (2), the equations for
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Fig. 6. The power control scheme used in this paper.

the solar panel inverter are augmented with the following exogenous input for the power setpoint

\[ P_{solar}(t) = P_{soc}(t), \]

where \( P_{solar}(t) \) is the available solar power at time \( t \).

Without any control over the loads and solar panel setpoint, the only components to be considered in the power setpoint control problem are the vehicle battery and generator. This is addressed in Section III-C.

Finally, the power balance at the buses is modeled as follows. Using phasor notation, the AC terminal voltages are given by

\[ V_{t_n} = V_{t_n}e^{j\theta_{t_n}}, \quad n = 1, 2, 3, 4, \]

where \( n \) is an index for the terminals. The inverter internal AC bus voltages \( V_{in} \) are similarly defined. The line impedances between the terminals are expressed as

\[ Z_{1,n} - R_{1,n} + jX_{1,n}, \quad n = 2, 3, 4. \]

The line and inverter currents are thus obtained as

\[ I_{1,n} = \frac{V_{t1} - V_{t_n}}{Z_{1,n}}, \quad n = 2, 3, 4, \]

\[ I_{inv1} = \frac{V_{t1} - V_{inv}}{jX}, \quad I_{inv2} = \frac{V_{inv2} - V_{inv}}{jX}. \]

The power balance equations are then

\[ I_{1,n} - I_{1,2} - I_{1,3} - I_{1,4} = 0 \]

\[ V_{t2}(I_{1,2} + I_{1,2}^*) + (P_{gen} + jQ_{gen}) = 0 \]

\[ V_{1,3}I_{1,3}^* - (P_{L3} + jQ_{L3}) = 0 \]

\[ V_{4}I_{1,4}^* - (P_{L4} + jQ_{L4}) = 0 \]

where asterisk denotes complex conjugate.

Based on the time-scale separation principle [30], the dynamics associated with the power electronics, which are on the order of milliseconds, are neglected when compared to the time scales of interest in this study, i.e., seconds.

B. Modeling the Power Sources and Loads

The drop in solar power (due to weather, malfunction, attack, etc.) is assumed to happen instantaneously and is thus modeled as a “worst case” step change as described by

\[ P_{solar}(t) = \begin{cases} P^1_{solar} & t \leq t_1 \\ P^2_{solar} & t > t_1 \end{cases}. \]

Based on the time constants reported in the literature for small diesel generators [31], the generator is assumed to have first order dynamics as given by

\[ \dot{\theta}_{gen} = \frac{1}{\tau_{gen}} (P_{set}^gen - P_{gen}). \]

with a discussion of \( P_{set}^gen \) provided in Section III-C.

The battery is modeled as a voltage source with an internal resistance. Within the time scale of interest (i.e., seconds), the change in the state-of-charge (SoC) is assumed to be negligible, and thus the SoC dependence of the open-circuit voltage (OCV) of the battery is neglected along with any other battery dynamics. We assume a string of batteries in series so that the nominal V_{OCV} at 50% charge is equal to the nominal DC bus voltage \( V_{batt} \). The battery is represented using the following relationship:

\[ V_{dc} = V_{OCV} - R_{batt}I_{inv}. \]

where \( I_{inv} \) is given by (2h), and is considered positive when the battery is discharging.

Finally, the loads are modeled as constant because they are assumed to be critical loads that need to be supplied continuously.

C. Power Control Structure

Within the considered framework, the only components whose power setpoints need to be managed are the vehicle battery and generator. The following feedback forms are proposed:

\[ P_{set}^{gen} = -k_1\omega_p - k_{I1} (P_{gen} - P_{cap}^{gen}) \]

\[ -k_1 \int \omega_p dt + P_{cap}^{gen}. \]

\[ P_{batt} = -k_2\omega_p + P_{batt}^{cap}. \]

where \( P_{cap} \) represents the pre-disturbance operating point.

Note that the first terms on the right hand side of the equations correspond to the traditional droop control scheme [1], [6], [32]–[35]. The second and third terms in the generator controller provide secondary frequency control with a PI control strategy. However, there is a minor difference from the typical PI control approach [36] in the sense that the P and I control actions act on two separate variables. Specifically, the second term in the generator controller adds a proportional feedback from the actual power output. This helps delay the response of the generator. A disturbance will then initially be compensated for mainly by the battery, helping save fuel. However, the battery cannot compensate for a large disturbance indefinitely due to its limited energy capacity. Hence, the generator controller also includes an integral action on the frequency deviation, so that any disturbance is
ultimately compensated for entirely by the generator. This control scheme ensures that in the post-disturbance steady state the frequency deviation is zero, thereby enabling the battery to return to its original operating condition, whereas the generator power output settles to

\[ P_{\text{gen}} = P_{\text{op}} + \frac{k_1 t}{1 + k_1} \int \omega_p dt. \]  

(12)

It is assumed that a higher-level dispatch controller exists that will eventually be informed about the disturbance and will determine the new (optimal) operating conditions for the generator and battery.

Also note the decentralized character of the controllers in (11). The only common signal to the controllers is the frequency deviation \( \omega_p \); the controllers are otherwise independent, use only the locally available information (i.e., frequency and local power), and do not require any communication with each other or any other component in the microgrid.

## D. Model Parameterization and Control Design

The microgrid system described above was simulated and optimized for the parameter values given in Table I. The parameters (and later results) that are given in the per-unit system can be converted to their absolute values using the base values reported in Table I. The parameter values for the inverter grid interface and inverter control gains are taken from [24]. The loads, step change in solar power, and the operating points for the battery and generator are obtained from a worst-case scenario of the optimal sizing and dispatch study as described in Section II. The maximum allowed frequency and voltage deviations were set to 0.5 Hz and 5%, respectively. The power regulation gains were tuned by linearizing the model around the given operating point and numerically solving an LQR problem with a constraint on frequency deviation and limits on the extent to which the power setpoints of the generator and battery could be moved. A further constraint ensures that the battery returns to its original state within 170 s to avoid draining the battery with subsequent energy extractions. The constraints were included with a large penalty in the optimization problem. Specifically, the objective function was formulated as

\[ J = \int_0^T \left( x^T Q x + u^T R u + C_{\text{lim}}(x, t) \right) dt \]  

(13)

with

\[ C_{\text{lim}}(x, t) = w_1 \left[ \max(x_1, 0) \right]^2 + w_2 \left[ \max(u_1, 0) \right]^2 + w_3 \left[ \max(u_2, 0) \right]^2 + w_4 \left[ \max(t - 170, 0) \right]^2 \]

where \( w_i \) are the weights, and \( x_{1,\text{lim}}, u_{1,\text{lim}}, \) and \( u_{2,\text{lim}} \) are the limits on frequency deviation, generator power, and battery power respectively. The resulting optimization problem was solved with an unconstrained nonlinear programming solver. The weights \( u_i \) were set equal, and progressively increased to a value of \( 10^8 \) in accordance with standard penalty function methods [37].

During the control design, the battery internal resistance was neglected and the battery was assumed to be a constant voltage source. Hence, voltage constraints were also neglected in the constrained LQR formulation.

## IV. Regulation Results and Discussion

The dynamic performance of the microgrid was explored by introducing a step change in the solar power production, as modeled by (8) with pre- and post-disturbance levels given in Table I. Figs. 7 and 8 show the frequency and voltage regulation performance of the controller. In these figures, the nonlinear microgrid model was used; however, the battery voltage was assumed to be constant to show the nominal performance of the controller. As the figures illustrate, both the frequency and voltage can be regulated successfully within the desired limits for this idealized battery voltage behavior.

Fig. 9 shows the battery and generator power trajectories during the disturbance. Initially the microgrid is stabilized using mainly the battery. Gradually the generator power is increased and, due to the integral action in the generator control scheme (11), the generator completely compensates for the solar power loss in the post-disturbance steady state, allowing the battery to return to its original charging state.

To check the impact of the constant battery voltage assumption on performance, the simulation was repeated with the battery internal resistance modeled with values varying from 0.1 to 1 \( \Omega \), in increments of 0.1 \( \Omega \). Fig. 10 shows the voltage regulation performance of the controller for select values of \( R_{\text{batt}} \). Voltage constraint violations occur at terminal 4 for \( R_{\text{batt}} \geq 0.3 \Omega \). Violations at other terminals are also observed for higher values of \( R_{\text{batt}} \). The corresponding battery voltages are shown in Fig. 11. The frequency regulation performance is not affected significantly by the range of \( R_{\text{batt}} \) values considered and thus the corresponding plot is not shown.

The voltage sensitivity displayed in Fig. 10 can be explained by considering the power balance across the microgrid. Because
the loads draw constant power, the total power supplied by the various sources must also remain effectively constant, though with some adjustment to account for changes in network losses. Therefore, when the solar power output reduces, the battery must take up the difference. This is not a controlled response, but rather a consequence of the power balance inherent in satisfying Kirchhoff’s laws. With battery internal resistance modeled, this sudden increase in the power delivered from the battery will cause a sharp decrease in the battery terminal voltage. This is apparent in Fig. 11. Controls quickly respond to restore the microgrid AC voltages though, as shown in Fig. 10.
The battery power needed to ensure satisfactory recovery from the loss of solar power is around 40 kW (Fig. 9). The maximum theoretical battery power available is

\[ P_{\text{batt}}^{\text{max}} = \frac{V_{\text{OC}}^2}{4R_{\text{batt}}} \]

which gives \( P_{\text{batt}}^{\text{max}} = 57.6 \text{ kW} \) for \( R_{\text{batt}} = 1 \Omega \). Hence, the battery is capable of providing the power needed, but cannot maintain the terminal voltages within desired limits.

The high sensitivity of voltage and low sensitivity of frequency to battery voltage fluctuations may seem to indicate that the voltage and frequency regulation problems are decoupled, implying the voltage control gain \( K_1 \) of the inverters may be increased to reduce the sensitivity of the voltages without affecting frequency regulation performance. However, Figs. 12 and 13 illustrate that this is not necessarily the case. These figures compare the regulation performance for the original value of \( K_1 = 10 \) and for a high gain of \( K_1 = 200 \). In both cases \( R_{\text{batt}} \) was set to 1 \( \Omega \). The higher controller gain greatly improves the voltage regulation performance and all terminal voltages are well within the desired limits. However, the frequency constraint is violated. To understand this frequency excursion, recall that the inverter control design, given by (2) and (11), introduces a droop characteristic that inversely couples power output and frequency\(^1\). The higher gain \( K_1 = 200 \) causes a higher overshoot in the power output than was the case with \( K_1 = 10 \). This larger power overshoot causes frequency to transiently undershoot its allowable limit, as shown in Fig. 12.

Therefore, it is critical to consider the voltage-current characteristics of the battery carefully and compensate for undesirable voltage drops either in the control design (e.g., by taking the battery characteristics into account and considering both frequency and voltage regulation together), or in the battery design (e.g., by changing battery chemistry, increasing battery size, and/or adding capacitors in parallel). The next section further considers the latter option, and in doing so closes the loop between the regulation and component sizing problems.

V. IMPLICATIONS FOR COMPONENT SIZING

The simulations presented in Section IV have been performed without considering any particular battery chemistry. However, in practice, the battery chemistry and configuration, i.e., number of battery cells in series and parallel, will dictate the internal resistance of the battery pack. The chemistry and configuration will also determine the energy capacity of the battery. Hence, it is of interest to study the extent to which regulation considerations can impact the energy capacity, i.e., the sizing, of the battery. This section considers the original inverter and setpoint control designs of Section III-D. Under that condition, Fig. 11 showed that a battery with \( R_{\text{batt}} = 0.1 \Omega \) yields satisfactory regulation performance.

As a representative battery for hybrid electric vehicle applications, an 11.1 V (3-cell) 5Ah Li-polymer battery is considered. The internal resistance of such a battery has been identified as 48.3 m\( \Omega \) [38]. To achieve a 480 V DC voltage supply for the inverter, 44 of these batteries should be connected in series. Furthermore, to achieve the 8.4 kWh battery capacity required by the optimal sizing solution mentioned in Section II, 4 parallel connections are required. This brings the capacity of the battery pack to 9.8 kWh.

On the other hand, with 44 series and 4 parallel connections, the total equivalent internal resistance of the battery pack is 0.53 \( \Omega \). This is above the desired value of 0.1 \( \Omega \) and in the range that leads to undesired voltage fluctuations as shown in Fig. 11. To bring the battery internal resistance down to 0.1 \( \Omega \), the number of parallel connections needs to be increased to 22, which in turn implies that the battery size increases from 9.8 kWh to 53.7 kWh.

This example highlights an important coupling between the component sizing and regulation problems. It shows that an optimal sizing study that considers only the energy capacity of the battery, e.g., [17]–[19], [22], [23], can potentially undersize the battery.

This undersizing issue is not only important for the battery, but also for the sizing of other components in the microgrid. As an example, if the 53.7 kWh minimum battery size is introduced into the optimization framework of Section II as an additional constraint, the solar panel size reduces from 89 kW to 87 kW to partially offset the increased capital cost of the batteries. Moreover, the annualized capital cost increases from

\(^1\)Because inverter-based microgrids do not have synchronous generation, there is no natural relationship between frequency and power balance. This familiar behavior must be established by control action.
$91,500 to $94,100, and the annual fuel use is estimated to increase from 143.8 kL to 146.1 kL. These results are summarized in Table II. The increased fuel use is due to the reduced solar panel power, showing a tradeoff of meeting the regulation requirements.

It is important to re-emphasize that these results are presented as an illustration rather than an ultimate solution. For example, the dynamics of the battery have been neglected for simplicity, including the dependence of OCV on SoC. While this may be an appropriate assumption over the short time scale of interest in this paper, the dependence of OCV on SoC could be a significant factor in other circumstances. If so, it would be important to consider the battery chemistry, as different types of batteries have different OCV-SoC characteristics. For chemistries such as Li-ion, the OCV-SoC curve is quite flat in the normal operating region, i.e., the OCV is rather insensitive to changes in SoC. In such cases, it would be reasonable to expect that regulation capability is similarly insensitive to SoC. Other chemistries may display a more pronounced dependence of OCV on SoC that could affect the regulation capability.

Other types of storage could also be considered, for example using capacitors to augment or replace the batteries. However, such analysis is beyond the scope of this paper and is left as future work. To reiterate, the main goal of this paper has been to identify the regulation-sizing coupling, emphasize its importance, and highlight the need for an integrated design approach of the form proposed in the paper. Hence, the particular solution considered in this section, that of increasing the battery size, is not to be interpreted as the only or optimal solution.

### VI. SUMMARY AND CONCLUSION

The paper considered a conceptual military microgrid that operates autonomously, i.e., without connection to a larger power grid. A solar panel, along with vehicle batteries and generators provide the power, while loads are assumed to be constant and uncontrollable. Leveraging a decentralized, phase-locked-loop based inverter control strategy, this paper has considered a power setpoint control algorithm for the batteries and generators. The controller is tuned assuming the battery voltage is constant. The impact of this assumption is tested by considering a range of values for the battery internal resistance.

The results show that the battery internal resistance can affect the performance of both frequency and voltage regulation. Thus, an effective inverter-based control design framework should consider both regulation problems together, as well as the voltage-current characteristics of the DC sources.

The results further illustrate the impact of regulation considerations on the sizing of the components in the microgrid. This is illustrated by considering an increase in the battery size as one potential solution. Hence, an important coupling between the component sizing and regulation problems is shown. This coupling implies that the typical approach, where the two problems are considered separately due to their disparate time scales, may lead to unsatisfactory designs. It is concluded that microgrid sizing, dispatch, and regulation problems should be considered concurrently using an integrated design framework.

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